# fastecdsa Documentation

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## CHAPTER 1

Installation

The only actively supported operating systems at this time are most Linux distros and OS X.

You can use pip: \$ pip install fastecds a or clone the repo and use \$ python setup.py install. Note that you need to have a C compiler (you can check this via e.g. \$ which gcc or \$ which clang). You also need to have GMP on your system as the underlying C code in this package includes the gmp.h header (and links against gmp via the -1gmp flag).

### 1.1 Installing Dependencies

### 1.1.1 Ubuntu / Debian

\$ sudo apt-get install gcc python-dev libgmp3-dev

### 1.1.2 RHEL / CentOS

\$ sudo yum install gcc python-devel gmp-devel

# CHAPTER 2

### fastecdsa

### 2.1 fastecdsa.curve

```
class fastecdsa.curve.Curve (name: str, p: int, a: int, b: int, q: int, gx: int, gy: int, oid: bytes = None)
```

Bases: object

Representation of an elliptic curve.

Defines a group for the arithmetic operations of point addition and scalar multiplication. Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

#### **Attributes:**

name (str): The name of the curve

p (int): The value of p in the curve equation.

a (int): The value of a in the curve equation.

b (int): The value of b in the curve equation.

q (int): The order of the base point of the curve.

oid (bytes): The object identifier of the curve.

G

The base point of the curve.

For the purposes of ECDSA this point is multiplied by a private key to obtain the corresponding public key. Make a property to avoid cyclic dependency of Point on Curve (a point lies on a curve) and Curve on Point (curves have a base point).

```
__init__ (name: str, p: int, a: int, b: int, q: int, gx: int, gy: int, oid: bytes = None)
Initialize the parameters of an elliptic curve.
```

WARNING: Do not generate your own parameters unless you know what you are doing or you could generate a curve severely less secure than you think. Even then, consider using a standardized curve for the sake of interoperability.

Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

### Args: name (string): The name of the curve p (int): The value of p in the curve equation. a (int): The value of a in the curve equation. b (int): The value of b in the curve equation. q (int): The order of the base point of the curve. gx (int): The x coordinate of the base point of the curve. gy (int): The y coordinate of the base point of the curve. oid (bytes): The object identifier of the curve. $\mathtt{repr}$ () $\to$ $\mathrm{str}$ Return repr(self). weakref\_ list of weak references to the object (if defined) evaluate (x: int) $\rightarrow int$ Evaluate the elliptic curve polynomial at 'x' **Args:** x (int): The position to evaluate the polynomial at **Returns:** int: the value of $(x^3 + ax + b) mod p$ classmethod get curve by oid(oid: bytes) Get a curve via it's object identifier. is\_point\_on\_curve (point: (<class 'int'>, <class 'int'>)) → bool Check if a point lies on this curve. The check is done by evaluating the curve equation $y^2 \equiv x^3 + ax + b \pmod{p}$ at the given point (x, y)with this curve's domain parameters (a, b, p). If the congruence holds, then the point lies on this curve. **Args:** point (long, long): A tuple representing the point P as an (x, y) coordinate pair. Returns: bool: True if the point lies on this curve, otherwise False.

### 2.2 fastecdsa.ecdsa

```
Bases: Exception

fastecdsa.ecdsa.sign (msg: MsgTypes, d: int, curve: fastecdsa.curve.Curve = P256, hashfunc=<built-in function openssl_sha256>, prehashed: bool = False)
Sign a message using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf for more information.

Args:

msg (strlbyteslbytearray): A message to be signed.
d (int): The ECDSA private key of the signer.
curve (fastecdsa.curve.Curve): The curve to be used to sign the message.
hashfunc (_hashlib.HASH): The hash function used to compress the message.
prehashed (bool): The message being passed has already been hashed by hashfunc.
```

```
fastecdsa.ecdsa.verify(sig: Tuple[int, int], msg: MsgTypes, Q: fastecdsa.point.Point, curve: fastecdsa.curve.Curve = P256, hashfunc=<br/>built-in function openssl_sha256>, prehashed: bool = False) \rightarrow bool
```

Verify a message signature using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf for more information.

#### Args:

```
sig (int, int): The signature for the message.

msg (strlbyteslbytearray): A message to be signed.

Q (fastecdsa.point.Point): The ECDSA public key of the signer.

curve (fastecdsa.curve.Curve): The curve to be used to sign the message.

hashfunc (_hashlib.HASH): The hash function used to compress the message.

prehashed (bool): The message being passed has already been hashed by hashfunc.
```

**Returns:** bool: True if the signature is valid, False otherwise.

#### Raises:

**fastecdsa.ecdsa.EcdsaError: If the signature or public key are invalid. Invalid signature** in this case means that it has values less than 1 or greater than the curve order.

### 2.3 fastecdsa.encoding

```
class fastecdsa.encoding.KeyEncoder
    Bases: object
```

Base class that any encoding class for EC keys should derive from.

All overriding methods should be static. If your key encoder writes binary data you must have a field named binary\_data set to True in order for keys to correctly read from and write to disk.

Base class that any encoding class for EC signatures should derive from.

All overriding methods should be static.

### 2.4 fastecdsa.encoding.der

```
class fastecdsa.encoding.der.DEREncoder

Bases: fastecdsa.encoding.SigEncoder

static decode_signature(sig: bytes) -> (<class 'int'>, <class 'int'>)

Decode an EC signature from serialized DER format as described in https://tools.ietf.org/html/rfc2459 (section 7.2.2) and as detailed by bip-0066

Returns (r,s)

static encode_signature(r: int, s: int) → bytes

Encode an EC signature in serialized DER format as described in https://tools.ietf.org/html/rfc2459 (section 7.2.2) and as detailed by bip-0066
```

Args: r, s

```
Returns: bytes: The DER encoded signature

exception fastecdsa.encoding.der.InvalidDerSignature
Bases: Exception

2.5 fastecdsa.encoding.pem
```

class fastecdsa.encoding.pem.PEMEncoder Bases: fastecdsa.encoding.KeyEncoder static decode private key (pemdata: str) -> (<class 'int'>, <class 'fastecdsa.point.Point'>) Decode an EC key as described in RFC 5915 and RFC 5480. **Args:** pemdata (bytes): A sequence of bytes representing an encoded EC key. Returns: (long, fastecdsa.point.Point): A private key, public key tuple. If the encoded key was a public key the first entry in the tuple is None. static decode\_public\_key(pemdata: str, curve:  $fastecdsa.curve.Curve = None) \rightarrow$ fastecdsa.point.Point Delegate to private key decoding but return only the public key static encode\_private\_key(d: int, Q: fastecdsa.point.Point = None,curve.  $fastecdsa.curve.Curve = None) \rightarrow str$ Encode an EC keypair as described in RFC 5915. Args: d (long): An ECDSA private key. Q (fastecdsa.point.Point): The ECDSA public key. curve (fastecdsa.curve.Curve): The curve that the private key is for. **Returns:** str: The ASCII armored encoded EC keypair.  $static encode\_public\_key(Q: fastecdsa.point.Point) \rightarrow str$ Encode an EC public key as described in RFC 5480.

## 2.6 fastecdsa.encoding.sec1

**Returns:** str: The ASCII armored encoded EC public key.

```
exception fastecdsa.encoding.sec1.InvalidSEC1PublicKey
Bases: Exception

class fastecdsa.encoding.sec1.SEC1Encoder
Bases: fastecdsa.encoding.KeyEncoder

static decode_public_key (key: bytes, curve: fastecdsa.curve.Curve) → fastecdsa.point.Point

Decode a public key as described in http://www.secg.org/SEC1-Ver-1.0.pdf in sections 2.3.3/2.3.4

uncompressed: 04 + x_bytes + y_bytes compressed: 02 or 03 + x_bytes

Args: key (bytes): public key encoded using the SEC1 format curve (fastecdsa.curve.Curve): Curve to use when decoding the public key

Returns: Point: The decoded public key

Raises: InvalidSEC1PublicKey
```

```
static encode_public_key (point: fastecdsa.point.Point, compressed: bool = True) \rightarrow bytes
```

Encode a public key as described in http://www.secg.org/SEC1-Ver-1.0.pdf

in sections 2.3.3/2.3.4 uncompressed: 04 + x\_bytes + y\_bytes compressed: 02 or 03 + x\_bytes

**Args:** point (fastecdsa.point.Point): Public key to encode compressed (bool): Set to False if you want an uncompressed format

**Returns:** bytes: The SEC1 encoded public key

### 2.7 fastecdsa.keys

```
fastecdsa.keys.export_key (key, curve: fastecdsa.curve.Curve = None, filepath: str = None, encoder=<class 'fastecdsa.encoding.pem.PEMEncoder'>)

Export a public or private EC key in PEM format.
```

#### **Args:**

```
key (fastecdsa.point.Point | int): A public or private EC key curve (fastecdsa.curve.Curve): The curve corresponding to the key (required if the key is a private key) filepath (str): Where to save the exported key. If None the key is simply printed. encoder (type): The class used to encode the key
```

fastecdsa.keys.gen\_keypair (curve: fastecdsa.curve.Curve)  $\rightarrow$  Tuple[int, fastecdsa.point.Point] Generate a keypair that consists of a private key and a public key.

The private key d is an integer generated via a cryptographically secure random number generator that lies in the range [1, n), where n is the curve order. The public key Q is a point on the curve calculated as Q = dG, where G is the curve's base point.

Args: curve (fastecdsa.curve.Curve): The curve over which the keypair will be calulated.

**Returns:** int, fastecdsa.point.Point: Returns a tuple with the private key first and public key second.

Generate a private key to sign data with.

The private key d is an integer generated via a cryptographically secure random number generator that lies in the range [1, n), where n is the curve order. The default random number generator used is /dev/urandom.

#### **Args:**

```
curve (fastecdsa.curve.Curve): The curve over which the key will be calulated. randfunc (function): A function taking one argument 'n' and returning a bytestring of n random bytes suitable for cryptographic use. The default is "os.urandom"
```

**Returns:** int: Returns a positive integer smaller than the curve order.

fastecdsa.keys.get\_public\_key (d:int, curve: fastecdsa.curve.Curve)  $\rightarrow$  fastecdsa.point.Point Generate a public key from a private key.

The public key Q is a point on the curve calculated as Q = dG, where d is the private key and G is the curve's base point.

#### Args:

```
d (long): An integer representing the private key.
curve (fastecdsa.curve.Curve): The curve over which the key will be calulated.
```

**Returns:** fastecdsa.point.Point: The public key, a point on the given curve.

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```
fastecdsa.keys.get_public_keys_from_sig(sig:
                                                                  (<class 'int'>, <class 'int'>),
                                                                                                      P256,
                                                                       fastecdsa.curve.Curve
                                                          curve:
                                                          hashfunc = \langle built-in function opens sl sha256 \rangle) \rightarrow
                                                          Tuple[fastecdsa.point.Point, fastecdsa.point.Point]
      Recover the public keys that can verify a signature / message pair.
      Args:
           sig (int, int): A ECDSA signature.
           msg (strlbyteslbytearray): The message corresponding to the signature.
           curve (fastecdsa.curve.Curve): The curve used to sign the message.
           hashfunc (_hashlib.HASH): The hash function used to compress the message.
      Returns:
           (fastecdsa.point.Point, fastecdsa.point.Point): The public keys that can verify the signature for the
                message.
fastecdsa.keys.import_key(filepath: str, curve: fastecdsa.curve.Curve = None, public: bool =
                                      False, decoder = \langle class \ 'fastecdsa.encoding.pem.PEMEncoder' \rangle) \rightarrow
                                      Tuple[Optional[int], fastecdsa.point.Point]
      Import a public or private EC key in PEM format.
      Args:
           filepath (str): The location of the key file
           public (bool): Indicates if the key file is a public key
           decoder (fastecdsa.encoding.KeyEncoder): The class used to parse the key
      Returns: (long, fastecdsa.point.Point): A (private key, public key) tuple. If a public key was imported then the
           first value will be None.
2.8 fastecdsa.point
exception fastecdsa.point.CurveMismatchError(curve1, curve2)
      Bases: Exception
        _init__ (curve1, curve2)
           Initialize self. See help(type(self)) for accurate signature.
           list of weak references to the object (if defined)
class fastecdsa.point.Point (x: int, y: int, curve=P256)
      Bases: object
      Representation of a point on an elliptic curve.
      Attributes:
           x (int): The x coordinate of the point.
           y (int): The y coordinate of the point.
           curve (Curve): The curve that the point lies on.
        _add__ (other)
           Add two points on the same elliptic curve.
           Args:
```

self (Point): a point P on the curve

```
other (Point): a point Q on the curve
    Returns: Point: A point R such that R = P + Q
\underline{\hspace{0.1cm}}eq\underline{\hspace{0.1cm}} (other) \rightarrow bool
    Return self==value.
init (x: int, y: int, curve=P256)
    Initialize a point on an elliptic curve.
    The x and y parameters must satisfy the equation y^2 \equiv x^3 + ax + b \pmod{p}, where a, b, and p are
    attributes of the curve parameter.
    Args:
         x (int): The x coordinate of the point.
         y (int): The y coordinate of the point.
         curve (Curve): The curve that the point lies on.
mul (scalar: int)
    Multiply a Point on an elliptic curve by an integer.
    Args:
         self (Point): a point P on the curve
         other (int): an integer d \in \mathbb{Z}_{\square} where q is the order of the curve that P is on
    Returns: Point: A point R such that R = P * d
 _neg___()
    Return the negation of a Point i.e. the points reflection over the x-axis.
    Args:
         self (Point): a point P on the curve
    Returns: Point: A point R = (P_x, -P_y)
 _radd___(other)
    Add two points on the same elliptic curve.
    Args:
         self (Point): a point P on the curve
         other (Point): a point Q on the curve
    Returns: Point: A point R such that R = R + Q
\mathtt{\underline{repr}} () \to str
    Return repr(self).
__rmul___(scalar: int)
    Multiply a Point on an elliptic curve by an integer.
    Args:
         self (Point): a point P on the curve
         other (long): an integer d \in \mathbb{Z}_{\mathbb{N}} where q is the order of the curve that P is on
    Returns: Point: A point R such that R = d * P
 _str___()
    Return str(self).
__sub___ (other)
    Subtract two points on the same elliptic curve.
```

```
Args: self (Point): a point P on the curve other (Point): a point Q on the curve Returns: Point: A point R such that R = P - Q weakref_
```

list of weak references to the object (if defined)

### 2.9 fastecdsa.util

```
class fastecdsa.util.RFC6979 (msg: bytes, x: int, q: int, hashfunc: Callable, prehashed: bool =
                                          False)
      Bases: object
      Generate a nonce per RFC6979.
      In order to avoid reusing a nonce with the same key when signing two different messages (which leaks the
      private key) RFC6979 provides a deterministic method for generating nonces. This is based on using a pseudo-
      random function (HMAC) to derive a nonce from the message and private key. More info here: http://tools.ietf.
      org/html/rfc6979.
      Attributes:
           msg (bytes): A message being signed.
           x (int): An ECDSA private key.
           q (int): The order of the generator point of the curve being used to sign the message.
           hashfunc (_hashlib.HASH): The hash function used to compress the message.
           prehashed (bool): Whether the signature is on a pre-hashed message.
      gen nonce()
           http://tools.ietf.org/html/rfc6979#section-3.2
fastecdsa.util.mod_sqrt (a: int, p: int) -> (<class 'int'>, <class 'int'>)
      Compute the square root of a \pmod{p}
      In other words, find a value x such that x^2 \equiv a \pmod{p}.
      Args:
           a (int): The value whose root to take.
           p (int): The prime whose field to perform the square root in.
      Returns: (int, int): the two values of x satisfying x^2 \equiv a \pmod{p}.
fastecdsa.util.msg_bytes (msg) \rightarrow bytes
      Return bytes in a consistent way for a given message.
      The message is expected to be either a string, bytes, or an array of bytes.
      Args:
           msg (strlbyteslbytearray): The data to transform.
      Returns: bytes: The byte encoded data.
      Raises: ValueError: If the data cannot be encoded as bytes.
```

fastecdsa.util.validate\_type (instance: object, expected\_type: type)

Validate that instance is an instance of the expected\_type.

### Args:

instance: The object whose type is being checked expected\_type: The expected type of instance

var\_name: The name of the object

Raises: TypeError: If instance is not of type expected\_type

2.9. fastecdsa.util

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