
fastecdsa Documentation

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CHAPTER 1

Installation

The only actively supported operating systems at this time are most Linux distros and OS X.

You can use pip: `$ pip install fastecdsa` or clone the repo and use `$ python setup.py install`. Note that you need to have a C compiler (you can check this via e.g. `$ which gcc` or `$ which clang`). You also need to have [GMP](#) on your system as the underlying C code in this package includes the `gmp.h` header (and links against gmp via the `-lgmp` flag).

1.1 Installing Dependencies

1.1.1 Ubuntu / Debian

```
$ sudo apt-get install gcc python-dev libgmp3-dev
```

1.1.2 RHEL / CentOS

```
$ sudo yum install gcc python-devel gmp-devel
```


2.1 fastecdsa.curve

class fastecdsa.curve.**Curve** (*name, p, a, b, q, gx, gy, oid=None*)

Bases: object

Representation of an elliptic curve.

Defines a group for the arithmetic operations of point addition and scalar multiplication. Currently only curves defined via the equation $y^2 \equiv x^3 + ax + b \pmod{p}$ are supported.

Attributes:

- name (string): The name of the curve
- p (long): The value of p in the curve equation.
- a (long): The value of a in the curve equation.
- b (long): The value of b in the curve equation.
- q (long): The order of the base point of the curve.
- oid (long): The object identifier of the curve.

G

The base point of the curve.

For the purposes of ECDSA this point is multiplied by a private key to obtain the corresponding public key. Make a property to avoid cyclic dependency of Point on Curve (a point lies on a curve) and Curve on Point (curves have a base point).

__init__ (*name, p, a, b, q, gx, gy, oid=None*)

Initialize the parameters of an elliptic curve.

WARNING: Do not generate your own parameters unless you know what you are doing or you could generate a curve severely less secure than you think. Even then, consider using a standardized curve for the sake of interoperability.

Currently only curves defined via the equation $y^2 \equiv x^3 + ax + b \pmod{p}$ are supported.

Args:

name (string): The name of the curve
 p (long): The value of p in the curve equation.
 a (long): The value of a in the curve equation.
 b (long): The value of b in the curve equation.
 q (long): The order of the base point of the curve.
 gx (long): The x coordinate of the base point of the curve.
 gy (long): The y coordinate of the base point of the curve.
 oid (str): The object identifier of the curve.

__repr__ ()

Return repr(self).

__weakref__

list of weak references to the object (if defined)

evaluate (x)

Evaluate the elliptic curve polynomial at 'x'

Args: x (int): The position to evaluate the polynomial at

Returns: int: the value of $(x^3 + ax + b) \bmod p$

classmethod get_curve_by_oid (oid)

Get a curve via it's object identifier.

is_point_on_curve (P)

Check if a point lies on this curve.

The check is done by evaluating the curve equation $y^2 \equiv x^3 + ax + b \pmod{p}$ at the given point (x, y) with this curve's domain parameters (a, b, p) . If the congruence holds, then the point lies on this curve.

Args: P (long, long): A tuple representing the point P as an (x, y) coordinate pair.

Returns: bool: True if the point lies on this curve, otherwise False.

2.2 fastecdsa.ecdsa

exception fastecdsa.ecdsa.EcdsaError (msg)

Bases: Exception

fastecdsa.ecdsa.sign (msg , d , $curve=P256$, $hashfunc=<\text{built-in function openssl_sha256}>$, $prehashed=False$)

Sign a message using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

Args:

msg (str|bytes|bytearray): A message to be signed.

d (long): The ECDSA private key of the signer.

curve (fastecdsa.curve.Curve): The curve to be used to sign the message.

hashfunc (_hashlib.HASH): The hash function used to compress the message.

fastecdsa.ecdsa.verify (sig , msg , Q , $curve=P256$, $hashfunc=<\text{built-in function openssl_sha256}>$)

Verify a message signature using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

Args:

`sig` (long, long): The signature for the message.
`msg` (str|bytes|bytearray): A message to be signed.
`Q` (fastecdsa.point.Point): The ECDSA public key of the signer.
`curve` (fastecdsa.curve.Curve): The curve to be used to sign the message.
`hashfunc` (_hashlib.HASH): The hash function used to compress the message.

Returns: bool: True if the signature is valid, False otherwise.

Raises:

fastecdsa.ecdsa.EcdsaError: If the signature or public key are invalid. Invalid signature in this case means that it has values less than 1 or greater than the curve order.

2.3 fastecdsa.encoding

class fastecdsa.encoding.KeyEncoder

Bases: object

Base class that any encoding class for EC keys should derive from.

All overriding methods should be static.

class fastecdsa.encoding.SigEncoder

Bases: object

Base class that any encoding class for EC signatures should derive from.

All overriding methods should be static.

2.4 fastecdsa.encoding.der

class fastecdsa.encoding.der.DEREncoder

Bases: *fastecdsa.encoding.SigEncoder*

static decode_signature(*sig*)

Decode an EC signature from serialized DER format as described in <https://tools.ietf.org/html/rfc2459> (section 7.2.2) and as detailed by bip-0066

Returns (r,s)

static encode_signature(*r, s*)

Encode an EC signature in serialized DER format as described in <https://tools.ietf.org/html/rfc2459> (section 7.2.2) and as detailed by bip-0066

Args: r, s

Returns: bytes: The DER encoded signature

exception fastecdsa.encoding.der.InvalidDerSignature

Bases: Exception

2.5 fastecdsa.encoding.pem

```
class fastecdsa.encoding.pem.PEMEncoder
    Bases: fastecdsa.encoding.KeyEncoder

    static decode_private_key (pemdata)
        Decode an EC key as described in RFC 5915 and RFC 5480.

        Args: pemdata (bytes): A sequence of bytes representing an encoded EC key.

        Returns: (long, fastecdsa.point.Point): A private key, public key tuple. If the encoded key was a public
            key the first entry in the tuple is None.

    static decode_public_key (pemdata, curve=None)
        Delegate to private key decoding but return only the public key

    static encode_private_key (d, Q=None, curve=None)
        Encode an EC keypair as described in RFC 5915.

        Args:
            d (long): An ECDSA private key.
            Q (fastecdsa.point.Point): The ECDSA public key.
            curve (fastecdsa.curve.Curve): The curve that the private key is for.

        Returns: str: The ASCII armored encoded EC keypair.

    static encode_public_key (Q)
        Encode an EC public key as described in RFC 5480.

        Returns: str: The ASCII armored encoded EC public key.
```

2.6 fastecdsa.encoding.sec1

```
exception fastecdsa.encoding.sec1.InvalidSEC1PublicKey
    Bases: Exception

class fastecdsa.encoding.sec1.SEC1Encoder
    Bases: fastecdsa.encoding.KeyEncoder

    static decode_public_key (key, curve)
        Decode a public key as described in http://www.secg.org/SEC1-Ver-1.0.pdf in sections 2.3.3/2.3.4
            compressed: 04 + x_bytes + y_bytes uncompressed: 02 or 03 + x_bytes

        Args: curve (Curve): Curve to use when decoding the public key key (bytes): public key encoded using
            the SEC1 format

        Returns: Point: The decoded public key

        Raises: InvalidSEC1PublicKey

    static encode_public_key (point, compressed=True)
        Encode a public key as described in http://www.secg.org/SEC1-Ver-1.0.pdf
            in sections 2.3.3/2.3.4 compressed: 04 + x_bytes + y_bytes uncompressed: 02 or 03 + x_bytes

        Args: compressed (bool): Set to False if you want an uncompressed format

        Returns: bytes: The SEC1 encoded public key
```

2.7 fastecdsa.keys

`fastecdsa.keys.export_key(key, curve=None, filepath=None, encoder=<class 'fastecdsa.encoding.pem.PEMEncoder'>)`

Export a public or private EC key in PEM format.

Args:

`key` (`fastecdsa.point.Point` | `long`): A public or private EC key
`curve` (`fastecdsa.curve.Curve`): The curve corresponding to the key (required if the key is a private key)
`filepath` (`str`): Where to save the exported key. If `None` the key is simply printed.
`encoder` (`fastecdsa.encoding.KeyEncoder`): The class used to encode the key

`fastecdsa.keys.gen_keypair(curve)`

Generate a keypair that consists of a private key and a public key.

The private key d is an integer generated via a cryptographically secure random number generator that lies in the range $[1, n)$, where n is the curve order. The public key Q is a point on the curve calculated as $Q = dG$, where G is the curve's base point.

Args: `curve` (`fastecdsa.curve.Curve`): The curve over which the keypair will be calculated.

Returns: `long`, `fastecdsa.point.Point`: Returns a tuple with the private key first and public key second.

`fastecdsa.keys.gen_private_key(curve, randfunc=<built-in function urandom>)`

Generate a private key to sign data with.

The private key d is an integer generated via a cryptographically secure random number generator that lies in the range $[1, n)$, where n is the curve order. The default random number generator used is `/dev/urandom`.

Args:

`curve` (`fastecdsa.curve.Curve`): The curve over which the key will be calculated.
`randfunc` (function): A function taking one argument 'n' and returning a bytestring of n random bytes suitable for cryptographic use. The default is "os.urandom"

Returns: `long`: Returns a positive integer smaller than the curve order.

`fastecdsa.keys.get_public_key(d, curve)`

Generate a public key from a private key.

The public key Q is a point on the curve calculated as $Q = dG$, where d is the private key and G is the curve's base point.

Args:

`d` (`long`): An integer representing the private key.
`curve` (`fastecdsa.curve.Curve`): The curve over which the key will be calculated.

Returns: `fastecdsa.point.Point`: The public key, a point on the given curve.

`fastecdsa.keys.get_public_keys_from_sig(sig, msg, curve=P256, hashfunc=<built-in function openssl_sha256>)`

Recover the public keys that can verify a signature / message pair.

Args:

`sig` (`long`, `long`): A ECDSA signature.
`msg` (`str`|`bytes`|`bytearray`): The message corresponding to the signature.
`curve` (`fastecdsa.curve.Curve`): The curve used to sign the message.
`hashfunc` (`_hashlib.HASH`): The hash function used to compress the message.

Returns:

(`fastecdsa.point.Point`, `fastecdsa.point.Point`): The public keys that can verify the signature for the message.

```
fastecdsa.keys.import_key(filepath, curve=None, public=False, decoder=<class  
                             'fastecdsa.encoding.pem.PEMEncoder'>)
```

Import a public or private EC key in PEM format.

Args:

filepath (str): The location of the key file

public (bool): Indicates if the key file is a public key

decoder (`fastecdsa.encoding.KeyEncoder`): The class used to parse the key

Returns: (long, `fastecdsa.point.Point`): A (private key, public key) tuple. If a public key was imported then the first value will be None.

2.8 fastecdsa.point

exception `fastecdsa.point.CurveMismatchError` (*curve1*, *curve2*)

Bases: `Exception`

`__init__` (*curve1*, *curve2*)

Initialize self. See `help(type(self))` for accurate signature.

`__weakref__`

list of weak references to the object (if defined)

class `fastecdsa.point.Point` (*x*, *y*, *curve=P256*)

Bases: `object`

Representation of a point on an elliptic curve.

Attributes:

x (long): The x coordinate of the point.

y (long): The y coordinate of the point.

curve (`Curve`): The curve that the point lies on.

`__add__` (*other*)

Add two points on the same elliptic curve.

Args:

self (`Point`): a point *P* on the curve

other (`Point`): a point *Q* on the curve

Returns: `Point`: A point *R* such that $R = P + Q$

`__eq__` (*other*)

Return `self==value`.

`__init__` (*x*, *y*, *curve=P256*)

Initialize a point on an elliptic curve.

The x and y parameters must satisfy the equation $y^2 \equiv x^3 + ax + b \pmod{p}$, where a, b, and p are attributes of the curve parameter.

Args:

x (long): The x coordinate of the point.

`y (long)`: The y coordinate of the point.
`curve (Curve)`: The curve that the point lies on.

__mul__ (*scalar*)

Multiply a *Point* on an elliptic curve by an integer.

Args:

`self (Point)`: a point P on the curve
`other (long)`: an integer $d \in \mathbb{Z}_q$ where q is the order of the curve that P is on

Returns: *Point*: A point R such that $R = P * d$

__neg__ ()

Return the negation of a *Point* i.e. the points reflection over the x-axis.

Args:

`self (Point)`: a point P on the curve

Returns: *Point*: A point $R = (P_x, -P_y)$

__radd__ (*other*)

Add two points on the same elliptic curve.

Args:

`self (Point)`: a point P on the curve
`other (Point)`: a point Q on the curve

Returns: *Point*: A point R such that $R = P + Q$

__repr__ ()

Return `repr(self)`.

__rmul__ (*scalar*)

Multiply a *Point* on an elliptic curve by an integer.

Args:

`self (Point)`: a point P on the curve
`other (long)`: an integer $d \in \mathbb{Z}_q$ where q is the order of the curve that P is on

Returns: *Point*: A point R such that $R = d * P$

__str__ ()

Return `str(self)`.

__sub__ (*other*)

Subtract two points on the same elliptic curve.

Args:

`self (Point)`: a point P on the curve
`other (Point)`: a point Q on the curve

Returns: *Point*: A point R such that $R = P - Q$

__weakref__

list of weak references to the object (if defined)

2.9 fastecdsa.util

class fastecdsa.util.RFC6979 (*msg, x, q, hashfunc*)

Bases: object

Generate a nonce per RFC6979.

In order to avoid reusing a nonce with the same key when signing two different messages (which leaks the private key) RFC6979 provides a deterministic method for generating nonces. This is based on using a pseudo-random function (HMAC) to derive a nonce from the message and private key. More info here: <http://tools.ietf.org/html/rfc6979>.

Attributes:

msg (string): A message being signed.

x (long): An ECDSA private key.

q (long): The order of the generator point of the curve being used to sign the message.

hashfunc (_hashlib.HASH): The hash function used to compress the message.

gen_nonce ()

<http://tools.ietf.org/html/rfc6979#section-3.2>

fastecdsa.util.mod_sqrt (*a, p*)

Compute the square root of $a \pmod{p}$

In other words, find a value x such that $x^2 \equiv a \pmod{p}$.

Args:

a (long): The value whose root to take.

p (long): The prime whose field to perform the square root in.

Returns: (long, long): the two values of x satisfying $x^2 \equiv a \pmod{p}$.

fastecdsa.util.msg_bytes (*msg*)

Return bytes in a consistent way for a given message.

The message is expected to be either a string, bytes, or an array of bytes.

Args:

msg (str|bytes|bytearray): The data to transform.

Returns: bytes: The byte encoded data.

Raises: ValueError: If the data cannot be encoded as bytes.

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