

---

# **fastecdsa Documentation**

***Release 1.6.4***

**Anton Kueltz**

**Apr 09, 2019**



---

## Contents:

---

<b>1</b>	<b>Installation</b>	<b>1</b>
1.1	Installing Dependencies . . . . .	1
<b>2</b>	<b>fastecdsa</b>	<b>3</b>
2.1	fastecdsa.asn1 . . . . .	3
2.2	fastecdsa.curve . . . . .	3
2.3	fastecdsa.ecdsa . . . . .	4
2.4	fastecdsa.keys . . . . .	5
2.5	fastecdsa.point . . . . .	6
2.6	fastecdsa.util . . . . .	8
	<b>Python Module Index</b>	<b>9</b>



# CHAPTER 1

---

## Installation

---

The only actively supported operating systems at this time are most Linux distros and OS X.

You can use pip: `$ pip install fastecdsa` or clone the repo and use `$ python setup.py install`. Note that you need to have a C compiler (you can check this via e.g. `$ which gcc` or `$ which clang`). You also need to have [GMP](#) on your system as the underlying C code in this package includes the `gmp.h` header (and links against gmp via the `-lgmp` flag).

## 1.1 Installing Dependencies

### 1.1.1 Ubuntu / Debian

```
$ sudo apt-get install gcc python-dev libgmp3-dev
```

### 1.1.2 RHEL / CentOS

```
$ sudo yum install gcc python-devel gmp-devel
```



## 2.1 fastecdsa.asn1

## 2.2 fastecdsa.curve

**class** fastecdsa.curve.**Curve** (*name, p, a, b, q, gx, gy, oid=None*)

Bases: object

Representation of an elliptic curve.

Defines a group for the arithmetic operations of point addition and scalar multiplication. Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

**Attributes:**

- name (string): The name of the curve
- p (long): The value of  $p$  in the curve equation.
- a (long): The value of  $a$  in the curve equation.
- b (long): The value of  $b$  in the curve equation.
- q (long): The order of the base point of the curve.
- oid (long): The object identifier of the curve.

**G**

The base point of the curve.

For the purposes of ECDSA this point is multiplied by a private key to obtain the corresponding public key. Make a property to avoid cyclic dependency of Point on Curve (a point lies on a curve) and Curve on Point (curves have a base point).

\_\_init\_\_ (*name, p, a, b, q, gx, gy, oid=None*)

Initialize the parameters of an elliptic curve.

**WARNING:** Do not generate your own parameters unless you know what you are doing or you could generate a curve severely less secure than you think. Even then, consider using a standardized curve for the sake of interoperability.

Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

**Args:**

name (string): The name of the curve  
 p (long): The value of  $p$  in the curve equation.  
 a (long): The value of  $a$  in the curve equation.  
 b (long): The value of  $b$  in the curve equation.  
 q (long): The order of the base point of the curve.  
 gx (long): The x coordinate of the base point of the curve.  
 gy (long): The y coordinate of the base point of the curve.  
 oid (str): The object identifier of the curve.

**\_\_repr\_\_** ()

Return repr(self).

**\_\_weakref\_\_**

list of weak references to the object (if defined)

**evaluate** (x)

Evaluate the elliptic curve polynomial at 'x'

**Args:** x (int): The position to evaluate the polynomial at

**Returns:** int: the value of  $(x^3 + ax + b) \bmod p$

**classmethod get\_curve\_by\_oid** (oid)

Get a curve via it's object identifier.

**is\_point\_on\_curve** (P)

Check if a point lies on this curve.

The check is done by evaluating the curve equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  at the given point  $(x, y)$  with this curve's domain parameters  $(a, b, p)$ . If the congruence holds, then the point lies on this curve.

**Args:** P (long, long): A tuple representing the point  $P$  as an  $(x, y)$  coordinate pair.

**Returns:** bool: True if the point lies on this curve, otherwise False.

## 2.3 fastecdsa.ecdsa

**exception fastecdsa.ecdsa.EcdsaError** (msg)

Bases: Exception

**fastecdsa.ecdsa.sign** (msg, d, curve=P256, hashfunc=<built-in function openssl\_sha256>)

Sign a message using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

**Args:**

msg (str|bytes|bytearray): A message to be signed.  
 d (long): The ECDSA private key of the signer.  
 curve (fastecdsa.curve.Curve): The curve to be used to sign the message.  
 hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**fastecdsa.ecdsa.verify** (sig, msg, Q, curve=P256, hashfunc=<built-in function openssl\_sha256>)

Verify a message signature using the elliptic curve digital signature algorithm.



The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

**Args:**

sig (long, long): The signature for the message.  
 msg (str|bytes|bytearray): A message to be signed.  
 Q (fastecdsa.point.Point): The ECDSA public key of the signer.  
 curve (fastecdsa.curve.Curve): The curve to be used to sign the message.  
 hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**Returns:** bool: True if the signature is valid, False otherwise.

**Raises:**

**fastecdsa.ecdsa.EcdsaError: If the signature or public key are invalid. Invalid signature** in this case means that it has values less than 1 or greater than the curve order.

## 2.4 fastecdsa.keys

`fastecdsa.keys.export_key(key, curve=None, filepath=None, encoder=<class 'fastecdsa.encoding.pem.PEMEncoder'>)`

Export a public or private EC key in PEM format.

**Args:**

key (fastecdsa.point.Point | long): A public or private EC key  
 curve (fastecdsa.curve.Curve): The curve corresponding to the key (required if the key is a private key)  
 filepath (str): Where to save the exported key. If None the key is simply printed.  
 encoder (fastecdsa.encoding.KeyEncoder): The class used to encode the key

`fastecdsa.keys.gen_keypair(curve)`

Generate a keypair that consists of a private key and a public key.

The private key  $d$  is an integer generated via a cryptographically secure random number generator that lies in the range  $[1, n)$ , where  $n$  is the curve order. The public key  $Q$  is a point on the curve calculated as  $Q = dG$ , where  $G$  is the curve's base point.

**Args:** curve (fastecdsa.curve.Curve): The curve over which the keypair will be calculated.

**Returns:** long, fastecdsa.point.Point: Returns a tuple with the private key first and public key second.

`fastecdsa.keys.gen_private_key(curve, randfunc=<built-in function urandom>)`

Generate a private key to sign data with.

The private key  $d$  is an integer generated via a cryptographically secure random number generator that lies in the range  $[1, n)$ , where  $n$  is the curve order. The default random number generator used is `/dev/urandom`.

**Args:** curve (fastecdsa.curve.Curve): The curve over which the key will be calculated. randfunc (function): A function taking one argument 'n' and returning a bytestring

of n random bytes suitable for cryptographic use. The default is "os.urandom"

**Returns:** long: Returns a positive integer smaller than the curve order.

`fastecdsa.keys.get_public_key(d, curve)`

Generate a public key from a private key.

The public key  $Q$  is a point on the curve calculated as  $Q = dG$ , where  $d$  is the private key and  $G$  is the curve's base point.

**Args:**

d (long): An integer representing the private key.  
 curve (fastecdsa.curve.Curve): The curve over which the key will be calculated.

**Returns:** fastecdsa.point.Point: The public key, a point on the given curve.

`fastecdsa.keys.get_public_keys_from_sig(sig, msg, curve=P256, hashfunc=<built-in function openssl_sha256>)`

Recover the public keys that can verify a signature / message pair.

**Args:**

sig (long, long): A ECDSA signature.  
 msg (str|bytes|bytearray): The message corresponding to the signature.  
 curve (fastecdsa.curve.Curve): The curve used to sign the message.  
 hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**Returns:**

(fastecdsa.point.Point, fastecdsa.point.Point): The public keys that can verify the signature for the message.

`fastecdsa.keys.import_key(filepath, curve=None, public=False, decoder=<class 'fastecdsa.encoding.pem.PEMEncoder'>)`

Import a public or private EC key in PEM format.

**Args:**

filepath (str): The location of the key file  
 public (bool): Indicates if the key file is a public key  
 decoder (fastecdsa.encoding.KeyEncoder): The class used to parse the key

**Returns:** (long, fastecdsa.point.Point): A (private key, public key) tuple. If a public key was imported then the first value will be None.

## 2.5 fastecdsa.point

**exception** fastecdsa.point.CurveMismatchError (curve1, curve2)

Bases: Exception

`__init__(curve1, curve2)`

Initialize self. See help(type(self)) for accurate signature.

`__weakref__`

list of weak references to the object (if defined)

**class** fastecdsa.point.Point (x, y, curve=P256)

Bases: object

Representation of a point on an elliptic curve.

**Attributes:**

x (long): The x coordinate of the point.  
 y (long): The y coordinate of the point.  
 curve (Curve): The curve that the point lies on.

`__add__(other)`

Add two points on the same elliptic curve.

**Args:**

self (*Point*): a point  $P$  on the curve  
 other (*Point*): a point  $Q$  on the curve

**Returns:** *Point*: A point  $R$  such that  $R = P + Q$

`__eq__` (*other*)

Return self==value.

`__init__` (*x*, *y*, *curve=P256*)

Initialize a point on an elliptic curve.

The  $x$  and  $y$  parameters must satisfy the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$ , where  $a$ ,  $b$ , and  $p$  are attributes of the curve parameter.

**Args:**

$x$  (long): The  $x$  coordinate of the point.  
 $y$  (long): The  $y$  coordinate of the point.  
 curve (*Curve*): The curve that the point lies on.

`__mul__` (*scalar*)

Multiply a *Point* on an elliptic curve by an integer.

**Args:**

self (*Point*): a point  $P$  on the curve  
 other (long): an integer  $d \in \mathbb{Z}_q$  where  $q$  is the order of the curve that  $P$  is on

**Returns:** *Point*: A point  $R$  such that  $R = P * d$

`__neg__` ()

Return the negation of a *Point* i.e. the points reflection over the  $x$ -axis.

**Args:**

self (*Point*): a point  $P$  on the curve

**Returns:** *Point*: A point  $R = (P_x, -P_y)$

`__radd__` (*other*)

Add two points on the same elliptic curve.

**Args:**

self (*Point*): a point  $P$  on the curve  
 other (*Point*): a point  $Q$  on the curve

**Returns:** *Point*: A point  $R$  such that  $R = P + Q$

`__repr__` ()

Return repr(self).

`__rmul__` (*scalar*)

Multiply a *Point* on an elliptic curve by an integer.

**Args:**

self (*Point*): a point  $P$  on the curve  
 other (long): an integer  $d \in \mathbb{Z}_q$  where  $q$  is the order of the curve that  $P$  is on

**Returns:** *Point*: A point  $R$  such that  $R = d * P$

**\_\_str\_\_** ()  
Return str(self).

**\_\_sub\_\_** (other)  
Subtract two points on the same elliptic curve.

**Args:**

- self (*Point*): a point  $P$  on the curve
- other (*Point*): a point  $Q$  on the curve

**Returns:** *Point*: A point  $R$  such that  $R = P - Q$

**\_\_weakref\_\_**  
list of weak references to the object (if defined)

## 2.6 fastecdsa.util

**class** fastecdsa.util.**RFC6979** (msg, x, q, hashfunc)  
Bases: object

Generate a nonce per RFC6979.

In order to avoid reusing a nonce with the same key when signing two different messages (which leaks the private key) RFC6979 provides a deterministic method for generating nonces. This is based on using a pseudo-random function (HMAC) to derive a nonce from the message and private key. More info here: <http://tools.ietf.org/html/rfc6979>.

**Attributes:**

- msg (string): A message being signed.
- x (long): An ECDSA private key.
- q (long): The order of the generator point of the curve being used to sign the message.
- hashfunc (`_hashlib.HASH`): The hash function used to compress the message.

**gen\_nonce** ()  
<http://tools.ietf.org/html/rfc6979#section-3.2>

fastecdsa.util.**mod\_sqrt** (a, p)  
Compute the square root of  $a \pmod{p}$

In other words, find a value  $x$  such that  $x^2 \equiv a \pmod{p}$ .

**Args:**

- a (long): The value whose root to take.
- p (long): The prime whose field to perform the square root in.

**Returns:** (long, long): the two values of  $x$  satisfying  $x^2 \equiv a \pmod{p}$ .

fastecdsa.util.**msg\_bytes** (msg)  
Return bytes in a consistent way for a given message.

The message is expected to be either a string, bytes, or an array of bytes.

**Args:**

- msg (str|bytes|bytearray): The data to transform.

**Returns:** bytes: The byte encoded data.

**Raises:** ValueError: If the data cannot be encoded as bytes.

### **f**

- `fastecdsa.curve`, 3
- `fastecdsa.ecdsa`, 4
- `fastecdsa.keys`, 5
- `fastecdsa.point`, 6
- `fastecdsa.util`, 8



## Symbols

`__add__()` (*fastecdsa.point.Point* method), 6  
`__eq__()` (*fastecdsa.point.Point* method), 7  
`__init__()` (*fastecdsa.curve.Curve* method), 3  
`__init__()` (*fastecdsa.point.CurveMismatchError* method), 6  
`__init__()` (*fastecdsa.point.Point* method), 7  
`__mul__()` (*fastecdsa.point.Point* method), 7  
`__neg__()` (*fastecdsa.point.Point* method), 7  
`__radd__()` (*fastecdsa.point.Point* method), 7  
`__repr__()` (*fastecdsa.curve.Curve* method), 4  
`__repr__()` (*fastecdsa.point.Point* method), 7  
`__rmul__()` (*fastecdsa.point.Point* method), 7  
`__str__()` (*fastecdsa.point.Point* method), 7  
`__sub__()` (*fastecdsa.point.Point* method), 8  
`__weakref__` (*fastecdsa.curve.Curve* attribute), 4  
`__weakref__` (*fastecdsa.point.CurveMismatchError* attribute), 6  
`__weakref__` (*fastecdsa.point.Point* attribute), 8

## C

*Curve* (class in *fastecdsa.curve*), 3  
*CurveMismatchError*, 6

## E

*EcdsaError*, 4  
`evaluate()` (*fastecdsa.curve.Curve* method), 4  
`export_key()` (in module *fastecdsa.keys*), 5

## F

*fastecdsa.curve* (module), 3  
*fastecdsa.ecdsa* (module), 4  
*fastecdsa.keys* (module), 5  
*fastecdsa.point* (module), 6  
*fastecdsa.util* (module), 8

## G

*G* (*fastecdsa.curve.Curve* attribute), 3  
`gen_keypair()` (in module *fastecdsa.keys*), 5

`gen_nonce()` (*fastecdsa.util.RFC6979* method), 8  
`gen_private_key()` (in module *fastecdsa.keys*), 5  
`get_curve_by_oid()` (*fastecdsa.curve.Curve* class method), 4  
`get_public_key()` (in module *fastecdsa.keys*), 5  
`get_public_keys_from_sig()` (in module *fastecdsa.keys*), 6

## I

`import_key()` (in module *fastecdsa.keys*), 6  
`is_point_on_curve()` (*fastecdsa.curve.Curve* method), 4

## M

`mod_sqrt()` (in module *fastecdsa.util*), 8  
`msg_bytes()` (in module *fastecdsa.util*), 8

## P

*Point* (class in *fastecdsa.point*), 6

## R

*RFC6979* (class in *fastecdsa.util*), 8

## S

`sign()` (in module *fastecdsa.ecdsa*), 4

## V

`verify()` (in module *fastecdsa.ecdsa*), 4