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# **fastecdsa Documentation**

***Release 1.6.4***

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# CHAPTER 1

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## Installation

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The only actively supported operating systems at this time are most Linux distros and OS X.

You can use pip: `$ pip install fastecdsa` or clone the repo and use `$ python setup.py install`. Note that you need to have a C compiler (you can check this via e.g. `$ which gcc` or `$ which clang`). You also need to have [GMP](#) on your system as the underlying C code in this package includes the `gmp.h` header (and links against gmp via the `-lgmp` flag).

## 1.1 Installing Dependencies

### 1.1.1 Ubuntu / Debian

```
$ sudo apt-get install gcc python-dev libgmp3-dev
```

### 1.1.2 RHEL / CentOS

```
$ sudo yum install gcc python-devel gmp-devel
```



## 2.1 fastecdsa.asn1

`fastecdsa.asn1.decode_key(pemdata)`

Decode an EC key as described in [RFC 5915](#) and [RFC 5480](#).

**Args:** pemdata (bytes): A sequence of bytes representing an encoded EC key.

**Returns:** (long, fastecdsa.point.Point): A private key, public key tuple. If the encoded key was a public key the first entry in the tuple is None.

`fastecdsa.asn1.encode_keypair(d, Q)`

Encode an EC keypair as described in [RFC 5915](#).

**Args:**

d (long): An ECDSA private key.

Q (fastecdsa.point.Point): The ECDSA public key.

**Returns:** str: The ASCII armored encoded EC keypair.

`fastecdsa.asn1.encode_public_key(Q)`

Encode an EC public key as described in [RFC 5480](#).

**Args:** Q (fastecdsa.point.Point): The ECDSA public key.

**Returns:** str: The ASCII armored encoded EC public key.

## 2.2 fastecdsa.curve

**class** `fastecdsa.curve.Curve` (name, p, a, b, q, gx, gy, oid=None)

Bases: object

Representation of an elliptic curve.

Defines a group for the arithmetic operations of point addition and scalar multiplication. Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

**Attributes:**

name (string): The name of the curve  
 p (long): The value of  $p$  in the curve equation.  
 a (long): The value of  $a$  in the curve equation.  
 b (long): The value of  $b$  in the curve equation.  
 q (long): The order of the base point of the curve.  
 oid (long): The object identifier of the curve.

**G**

The base point of the curve.

For the purposes of ECDSA this point is multiplied by a private key to obtain the corresponding public key. Make a property to avoid cyclic dependency of Point on Curve (a point lies on a curve) and Curve on Point (curves have a base point).

**\_\_init\_\_** (*name, p, a, b, q, gx, gy, oid=None*)

Initialize the parameters of an elliptic curve.

**WARNING:** Do not generate your own parameters unless you know what you are doing or you could generate a curve severely less secure than you think. Even then, consider using a standardized curve for the sake of interoperability.

Currently only curves defined via the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  are supported.

**Args:**

name (string): The name of the curve  
 p (long): The value of  $p$  in the curve equation.  
 a (long): The value of  $a$  in the curve equation.  
 b (long): The value of  $b$  in the curve equation.  
 q (long): The order of the base point of the curve.  
 gx (long): The x coordinate of the base point of the curve.  
 gy (long): The y coordinate of the base point of the curve.  
 oid (str): The object identifier of the curve.

**\_\_repr\_\_** ()

Return repr(self).

**\_\_weakref\_\_**

list of weak references to the object (if defined)

**classmethod get\_curve\_by\_oid** (*oid*)

Get a curve via it's object identifier.

**is\_point\_on\_curve** (*P*)

Check if a point lies on this curve.

The check is done by evaluating the curve equation  $y^2 \equiv x^3 + ax + b \pmod{p}$  at the given point  $(x, y)$  with this curve's domain parameters  $(a, b, p)$ . If the congruence holds, then the point lies on this curve.

**Args:** P (long, long): A tuple representing the point  $P$  as an  $(x, y)$  coordinate pair.

**Returns:** bool: True if the point lies on this curve, otherwise False.



## 2.3 fastecdsa.ecdsa

**exception** fastecdsa.ecdsa.EcdsaError(msg)

Bases: Exception

fastecdsa.ecdsa.**sign**(msg, d, curve=P256, hashfunc=<built-in function openssl\_sha256>)

Sign a message using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

**Args:**

msg (str): A message to be signed.

d (long): The ECDSA private key of the signer.

curve (fastecdsa.curve.Curve): The curve to be used to sign the message.

hashfunc (\_hashlib.HASH): The hash function used to compress the message.

fastecdsa.ecdsa.**verify**(sig, msg, Q, curve=P256, hashfunc=<built-in function openssl\_sha256>)

Verify a message signature using the elliptic curve digital signature algorithm.

The elliptic curve signature algorithm is described in full in FIPS 186-4 Section 6. Please refer to <http://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.186-4.pdf> for more information.

**Args:**

sig (long, long): The signature for the message.

msg (str): A message to be signed.

Q (fastecdsa.point.Point): The ECDSA public key of the signer.

curve (fastecdsa.curve.Curve): The curve to be used to sign the message.

hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**Returns:** bool: True if the signature is valid, False otherwise.

**Raises:**

**fastecdsa.ecdsa.EcdsaError: If the signature or public key are invalid. Invalid signature** in this case means that it has values less than 1 or greater than the curve order.

## 2.4 fastecdsa.keys

fastecdsa.keys.**export\_key**(key, curve=None, filepath=None)

Export a public or private EC key in PEM format.

**Args:**

key (fastecdsa.point.Point | long): A public or private EC key

curve (fastecdsa.curve.Curve): The curve corresponding to the key (required if the key is a private key)

filepath (str): Where to save the exported key. If None the key is simply printed.

fastecdsa.keys.**gen\_keypair**(curve)

Generate a keypair that consists of a private key and a public key.

The private key  $d$  is an integer generated via a cryptographically secure random number generator that lies in the range  $[1, n)$ , where  $n$  is the curve order. The public key  $Q$  is a point on the curve calculated as  $Q = dG$ , where  $G$  is the curve's base point.

**Args:** curve (fastecdsa.curve.Curve): The curve over which the keypair will be calculated.

**Returns:** long, fastecdsa.point.Point: Returns a tuple with the private key first and public key second.

`fastecdsa.keys.gen_private_key (curve)`

Generate a private key to sign data with.

The private key  $d$  is an integer generated via a cryptographically secure random number generator that lies in the range  $[1, n)$ , where  $n$  is the curve order. The specific random number generator used is `/dev/urandom`.

**Args:** curve (fastecdsa.curve.Curve): The curve over which the key will be calculated.

**Returns:** long: Returns a positive integer smaller than the curve order.

`fastecdsa.keys.get_public_key (d, curve)`

Generate a public key from a private key.

The public key  $Q$  is a point on the curve calculated as  $Q = dG$ , where  $d$  is the private key and  $G$  is the curve's base point.

**Args:**

d (long): An integer representing the private key.

curve (fastecdsa.curve.Curve): The curve over which the key will be calculated.

**Returns:** fastecdsa.point.Point: The public key, a point on the given curve.

`fastecdsa.keys.get_public_keys_from_sig (sig, msg, curve=P256, hashfunc=<built-in function openssl_sha256>)`

Recover the public keys that can verify a signature / message pair.

**Args:**

sig (long, long): A ECDSA signature.

msg (str): The message corresponding to the signature.

curve (fastecdsa.curve.Curve): The curve used to sign the message.

hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**Returns:**

(fastecdsa.point.Point, fastecdsa.point.Point): The public keys that can verify the signature for the message.

`fastecdsa.keys.import_key (filepath)`

Import a public or private EC key in PEM format.

**Args:** filepath (str): The location of the key file

**Returns:** (long, fastecdsa.point.Point): A (private key, public key) tuple. If a public key was imported then the first value will be None.

## 2.5 fastecdsa.point

**exception** fastecdsa.point.CurveMismatchError (curve1, curve2)

Bases: Exception

`__init__ (curve1, curve2)`

Initialize self. See help(type(self)) for accurate signature.

`__weakref__`

list of weak references to the object (if defined)

**class** fastecdsa.point.**Point** (*x*, *y*, *curve*=P256)

Bases: object

Representation of a point on an elliptic curve.

**Attributes:**

*x* (long): The x coordinate of the point.

*y* (long): The y coordinate of the point.

*curve* (Curve): The curve that the point lies on.

**\_\_add\_\_** (*other*)

Add two points on the same elliptic curve.

**Args:**

*self* (Point): a point *P* on the curve

*other* (Point): a point *Q* on the curve

**Returns:** Point: A point *R* such that  $R = P + Q$

**\_\_eq\_\_** (*other*)

Return self==value.

**\_\_init\_\_** (*x*, *y*, *curve*=P256)

Initialize a point on an elliptic curve.

The *x* and *y* parameters must satisfy the equation  $y^2 \equiv x^3 + ax + b \pmod{p}$ , where *a*, *b*, and *p* are attributes of the curve parameter.

**Args:**

*x* (long): The x coordinate of the point.

*y* (long): The y coordinate of the point.

*curve* (Curve): The curve that the point lies on.

**\_\_mul\_\_** (*scalar*)

Multiply a Point on an elliptic curve by an integer.

**Args:**

*self* (Point): a point *P* on the curve

*other* (long): an integer  $d \in \mathbb{Z}_q$  where *q* is the order of the curve that *P* is on

**Returns:** Point: A point *R* such that  $R = P * d$

**\_\_neg\_\_** ()

Return the negation of a Point i.e. the points reflection over the x-axis.

**Args:**

*self* (Point): a point *P* on the curve

**Returns:** Point: A point  $R = (P_x, -P_y)$

**\_\_radd\_\_** (*other*)

Add two points on the same elliptic curve.

**Args:**

*self* (Point): a point *P* on the curve

*other* (Point): a point *Q* on the curve

**Returns:** Point: A point *R* such that  $R = P + Q$

**\_\_repr\_\_()**  
Return repr(self).

**\_\_rmul\_\_ (scalar)**  
Multiply a *Point* on an elliptic curve by an integer.

**Args:**

self (*Point*): a point  $P$  on the curve  
other (long): an integer  $d \in \mathbb{Z}_q$  where  $q$  is the order of the curve that  $P$  is on

**Returns:** *Point*: A point  $R$  such that  $R = d * P$

**\_\_str\_\_()**  
Return str(self).

**\_\_sub\_\_ (other)**  
Subtract two points on the same elliptic curve.

**Args:**

self (*Point*): a point  $P$  on the curve  
other (*Point*): a point  $Q$  on the curve

**Returns:** *Point*: A point  $R$  such that  $R = P - Q$

**\_\_weakref\_\_**  
list of weak references to the object (if defined)

## 2.6 fastecdsa.util

**class** fastecdsa.util.**RFC6979** (*msg, x, q, hashfunc*)  
Bases: object

Generate a nonce per RFC6979.

In order to avoid reusing a nonce with the same key when signing two different messages (which leaks the private key) RFC6979 provides a deterministic method for generating nonces. This is based on using a pseudo-random function (HMAC) to derive a nonce from the message and private key. More info here: <http://tools.ietf.org/html/rfc6979>.

**Attributes:**

msg (string): A message being signed.  
x (long): An ECDSA private key.  
q (long): The order of the generator point of the curve being used to sign the message.  
hashfunc (\_hashlib.HASH): The hash function used to compress the message.

**gen\_nonce()**  
<http://tools.ietf.org/html/rfc6979#section-3.2>

fastecdsa.util.**mod\_sqrt** (*a, p*)  
Compute the square root of  $a \pmod{p}$

In other words, find a value  $x$  such that  $x^2 \equiv a \pmod{p}$ .

**Args:**

a (long): The value whose root to take.  
p (long): The prime whose field to perform the square root in.

**Returns:** (long, long): the two values of  $x$  satisfying  $x^2 \equiv a \pmod{p}$ .



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